

Draft:
Deep Learning in Neural Networks: An Overview

Technical Report IDSIA-03-14

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17 April 2014

Abstract

In recent years, deep neural networks (including recurrent ones) have won numerous contests in pattern recognition and machine learning. This historical survey compactly summarises relevant work, much of it from the previous millennium. Shallow and deep learners are distinguished by the depth of their *credit assignment paths*, which are chains of possibly learnable, causal links between actions and effects. I review deep supervised learning (also recapitulating the history of backpropagation), unsupervised learning, reinforcement learning & evolutionary computation, and indirect search for short programs encoding deep and large networks.

Preface

This is the draft of an invited *Deep Learning* (DL) overview. One of its goals is to assign credit to those who contributed to the present state of the art. I acknowledge the limitations of attempting to achieve this goal. The DL research community itself may be viewed as a continually evolving, deep network of scientists who have influenced each other in complex ways. Starting from recent DL results, I tried to trace back the origins of relevant ideas through the past half century and beyond, sometimes using “local search” to follow citations of citations backwards in time. Since not all DL publications properly acknowledge earlier relevant work, additional global search strategies were employed, aided by consulting numerous neural network experts. As a result, the present draft mostly consists of references (about 600 entries so far). Nevertheless, through an expert selection bias I may have missed important work. A related bias was surely introduced by my special familiarity with the work of my own DL research group in the past quarter-century. For these reasons, the present draft should be viewed as merely a snapshot of an ongoing credit assignment process. To help improve it, please do not hesitate to send corrections and suggestions to juergen@idsia.ch.

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1 Introduction

Which modifiable components of a learning system are responsible for its success or failure? What changes to them improve performance? This has been called the *fundamental credit assignment problem* (Minsky, 1963). There are general credit assignment methods for *universal problem solvers* that are time-optimal in various theoretical senses (Sec. 6.8). The present survey, however, will focus on the narrower, but now commercially important, subfield of *Deep Learning (DL) in Artificial Neural Networks (NNs)*. We are interested in accurate credit assignment across possibly *many*, often nonlinear, computational stages of NNs.

Shallow NN-like models have been around for many decades if not centuries (Sec. 5.1). NNs with several successive non-linear layers of neurons date back at least to the late 1970s (Sec. 5.4). An efficient gradient descent method for teacher-based *Supervised Learning (SL)* in discrete, differentiable networks of arbitrary depth called *backpropagation (BP)* was developed in the 1960s and 1970s, and applied to NNs in 1981 (Sec. 5.4). BP-based training of *deep* NNs with *many* layers, however, had been found to be difficult in practice by the late 1980s (Sec. 5.6), and become an explicit research subject by the early 1990s (Sec. 5.8). DL became practically feasible to some extent through the help of *Unsupervised Learning (UL)*, e.g., (Sec. 5.9, 5.14). The 1990s and 2000s also saw many improvements of purely supervised DL (Sec. 5). In the new millennium, deep NNs have finally attracted wide-spread attention, mainly by outperforming alternative machine learning methods such as kernel machines (Vapnik, 1995; Schölkopf et al., 1998) in numerous important applications. In fact, supervised deep NNs have won numerous recent official international pattern recognition competitions (e.g., Sec. 5.15, 5.17, 5.19, 5.20), achieving the first superhuman visual pattern recognition results in limited domains (Sec. 5.17). Deep NNs also have become relevant for the more general field of *Reinforcement Learning (RL)* where there is no supervising teacher (Sec. 6).

Both *feedforward* (acyclic) NNs (FNNs) and *recurrent* (cyclic) NNs (RNNs) have won contests (Sec. 5.10, 5.13, 5.15, 5.17, 5.19, 5.20). RNNs are general computers more powerful than FNNs, and can in principle encode memories of arbitrary sequences of input patterns, e.g., (Siegelmann and Sontag, 1991; Schmidhuber, 1990a). The rest of this paper is structured as follows. Sec. 2 introduces a compact, event-oriented notation that is simple yet general enough to accommodate both FNNs and RNNs. Sec. 3 introduces the concept of *Credit Assignment Paths (CAPs)* to measure whether learning in a given NN application is of the *deep* or *shallow* type. Sec. 4 lists recurring themes of DL in SL, UL, and RL. Sec. 5 focuses on SL and UL, and on how UL can facilitate SL, although pure SL has become dominant in recent competitions (Sec. 5.15-5.20). Sec. 5 is arranged in a historical timeline format with subsections on important inspirations and technical contributions. Sec. 6 on deep RL discusses traditional *Dynamic Programming (DP)*-based RL combined with gradient-based search techniques for SL or UL in deep NNs, as well as general methods for direct and indirect search in the weight space of deep FNNs and RNNs, including successful policy gradient and evolutionary methods.

2 Event-Oriented Notation for Activation Spreading in FNNs/RNNs

Throughout this paper, let i, j, k, t, p, q, r denote positive integer variables assuming ranges implicit in the given contexts. Let n, m, T denote positive integer constants.

An NN's topology may change over time, e.g., (Fahlman, 1991; Fritzsche, 1994). At any given moment, it can be described as a finite subset of units (or nodes or neurons) $N = \{u_1, u_2, \dots\}$ and a finite set $H \subseteq N \times N$ of directed edges or connections between nodes. FNNs are acyclic graphs, RNNs cyclic. The first (input) layer is the set of input units, a subset of N . In FNNs, the k -th layer ($k > 1$) is the set of all nodes $u \in N$ such that there is an edge path of length $k - 1$ (but no longer path) between some input unit and u . (There may be shortcut connections between distant layers.)

The NN's behavior or program is determined by a set of real-valued, possibly modifiable, parameters or weights w_i ($i = 1, \dots, n$). We now focus on a single finite *episode* or *epoch* of information processing and activation spreading, without learning through weight changes. The following slightly unconventional notation is designed to compactly describe what is happening *during the runtime* of the system.

During an episode, there is a *partially causal sequence* x_t ($t = 1, \dots, T$) of real values that I call

events. Each x_t is either an input set by the environment, or the activation of a unit that may directly depend on other $x_k (k < t)$ through a current NN topology-dependent set in_t of indices k representing incoming causal connections or links. Let the function v encode topology information and map such event index pairs (k, t) to weight indices. For example, in the non-input case we may have $x_t = f_t(net_t)$ with real-valued $net_t = \sum_{k \in in_t} x_k w_{v(k,t)}$ (additive case) or $net_t = \prod_{k \in in_t} x_k w_{v(k,t)}$ (multiplicative case), where f_t is a typically nonlinear real-valued function such as \tanh . In many recent competition-winning NNs (Sec. 5.17, 5.19, 5.20) there also are events of the type $x_t = \max_{k \in in_t} (x_k)$. x_t may directly affect certain $x_k (k > t)$ through outgoing connections or links represented through a current set out_t of indices k with $t \in in_k$. Some non-input events are called *output events*.

Note that many of the x_t may refer to different, time-varying activations of the *same* unit in sequence-processing RNNs, e.g., (Williams, 1989, “*unfolding in time*”), or also in FNNs sequentially exposed to time-varying input patterns of a large training set encoded as input events. During an episode, the same weight may get reused over and over again in topology-dependent ways, e.g., in RNNs, or in convolutional NNs (Sec. 5.3, 5.5). I call this weight sharing *across space and/or time*. Weight sharing may greatly reduce the NN’s descriptive complexity, which is the number of bits of information required to describe the NN.

In *Supervised Learning* (SL), certain NN output events x_t may be associated with teacher-given, real-valued labels or targets d_t yielding errors e_t , e.g., $e_t = 1/2(x_t - d_t)^2$. A typical goal of supervised NN training is to find weights that yield episodes with small total error E , the sum of all such e_t . The hope is that the NN will generalize well in later episodes, causing only small errors on previously unseen sequences of input events. Many alternative error functions for SL and UL are possible.

SL assumes that input events are independent of earlier output events (which may affect the environment through actions causing subsequent perceptions). This simplifying assumption does not hold in the broader fields of *Sequential Decision Making* and *Reinforcement Learning* (RL) (Kaelbling et al., 1996; Sutton and Barto, 1998; Hutter, 2005) (Sec. 6). In RL, some of the input events may encode real-valued reward signals given by the environment, and a typical goal is to find weights that yield episodes with a high sum of reward signals, through sequences of appropriate output actions.

Sec. 5.4 will use the notation above to compactly describe a central algorithm of DL, namely, back-propagation (BP) for supervised weight-sharing FNNs and RNNs. (FNNs may be viewed as RNNs with certain fixed zero weights.) Sec. 6 will address the more general RL case.

3 Depth of Credit Assignment Paths (CAPs) and of Problems

To measure whether credit assignment in a given NN application is of the *deep* or *shallow* type, I introduce the concept of *Credit Assignment Paths* or CAPs, which are chains of possibly causal links between events.

Let us first focus on SL. Consider two events x_p and x_q ($1 \leq p < q \leq T$). Depending on the application, they may have a *Potential Direct Causal Connection* (PDCC) expressed by the Boolean predicate $pdcc(p, q)$, which is true if and only if $p \in in_q$. Then the 2-element list (p, q) is defined to be a CAP from p to q (a minimal one). A learning algorithm may be allowed to change $w_{v(p,q)}$ to improve performance in future episodes.

More general, possibly indirect, *Potential Causal Connections* (PCC) are expressed by the recursively defined Boolean predicate $pcc(p, q)$, which in the SL case is true only if $pdcc(p, q)$, or if $pcc(p, k)$ for some k and $pdcc(k, q)$. In the latter case, appending q to any CAP from p to k yields a CAP from p to q (this is a recursive definition, too). The set of such CAPs may be large but is finite. Note that the same weight may affect many different PDCCs between successive events listed by a given CAP, e.g., in the case of RNNs, or weight-sharing FNNs.

Suppose a CAP has the form (\dots, k, t, \dots, q) , where k and t (possibly $t = q$) are the first successive elements with *modifiable* $w_{v(k,t)}$. Then the length of the suffix list (t, \dots, q) is called the CAP’s *depth* (which is 0 if there are no modifiable links at all). This depth limits how far backwards credit assignment can move down the causal chain to find a modifiable weight.¹

Suppose an episode and its event sequence x_1, \dots, x_T satisfy a computable criterion used to decide whether a given problem has been solved (e.g., total error E below some threshold). Then the set of

¹An alternative would be to count only *modifiable* links when measuring depth. In many typical NN applications this would not make a difference, but in some it would, e.g., Sec. 6.1.

used weights is called a *solution* to the problem, and the depth of the deepest CAP within the sequence is called the *solution's depth*. There may be other solutions (yielding different event sequences) with different depths. Given some fixed FNN or RNN topology, the smallest depth of any solution is called the *problem's depth*.

Sometimes we also speak of the *depth* of an architecture: SL FNNs with fixed topology imply a problem-independent maximal problem depth, typically the number of non-input layers. Similar for certain SL RNNs (Jaeger, 2001; Maass et al., 2002; Jaeger, 2004; Schrauwen et al., 2007) with fixed weights for all connections except those to output units—their maximal problem depth is 1, because only the final links in the corresponding CAPs are modifiable.

Note that the definitions above are solely based on the depths of causal chains, and agnostic of the temporal distance between events. For example, *shallow* FNNs perceiving large “time windows” of input events may correctly classify *long* input sequences through appropriate output events, and thus solve *shallow* problems involving *long* time lags between relevant events.

At which problem depth does *Shallow Learning* end, and *Deep Learning* begin? Discussions with DL experts have not yet yielded a conclusive answer to this question. Let me define for the purposes of this overview: problems of depth > 10 require *Very Deep Learning*.

The *difficulty* of a problem may have little to do with its depth. Some NNs can quickly learn to solve certain deep problems, e.g., through random weight guessing (Sec. 5.8) or other types of direct search (Sec. 6.6) or indirect search (Sec. 6.7) in weight space, or through collapsing sequences of (non)linear operations into a single (non)linear operation, or through training an NN first on shallow problems whose solutions may then generalize to deep problems,

Above we have focused on SL. In the more general case of RL in unknown environments, $pcc(p, q)$ is also true if x_p is an output event and x_q any later input event—any action may affect the environment and thus any later perception. (In the real world, the environment may even influence *non-input* events computed on a physical hardware entangled with the entire universe, but this is ignored here.) It is possible to model and replace such unmodifiable *environmental* PCCs through a part of the NN that has already learned to predict (through some of its units) input events from former input events and actions (Sec. 6.1). Its weights are frozen, but can help to assign credit to other, still modifiable weights used to compute actions (Sec. 6.1). This approach may lead to very deep CAPs though.

Some DL research is about automatically rephrasing problems such that their depth is reduced (Sec. 4). In particular, sometimes UL is used to make SL problems less deep, e.g., Sec. 5.9. Often *Dynamic Programming* (Sec. 4.1) is used to facilitate certain traditional RL problems, e.g., Sec. 6.2. Sec. 5 focuses on CAPs for SL, Sec. 6 on the more complex case of RL.

4 Recurring Themes of Deep Learning (DL)

4.1 Dynamic Programming (DP) for DL

One recurring theme of DL is *Dynamic Programming* (DP) (Bellman, 1957), which can help to facilitate credit assignment under certain assumptions. For example, in SL NNs, backpropagation itself can be viewed as a DP-derived method (Sec. 5.4). In traditional RL based on strong Markovian assumptions, DP-derived methods can help to greatly reduce problem depth (Sec. 6.2). DP algorithms are also essential for systems that combine graphical models (Dempster et al., 1977) such as *Hidden Markov Models* (HMMs) and NNs, e.g., (Bottou, 1991; Bengio, 1991; Bourlard and Morgan, 1994; Jordan and Sejnowski, 2001; Bishop, 2006; Dahl et al., 2012; Hinton et al., 2012a).

4.2 Unsupervised Learning (UL) Facilitating Supervised Learning (SL) and RL

Another recurring theme is how UL can facilitate both SL (Sec. 5) and RL (Sec. 6). UL (Sec. 5.6.4) is normally used to encode raw incoming data such as video or speech streams in a form that is more convenient for subsequent goal-directed learning. In particular, codes that describe the original data in a less redundant or more compact way can be fed into SL (Sec. 5.9, 5.14) or RL machines (Sec. 6.4), whose

search spaces may thus become smaller (and whose CAPs shallower) than those necessary for dealing with the raw data. UL is closely connected to the topics of *regularization* and compression (Sec. 4.3).

4.3 Occam's Razor: Compression and Minimum Description Length (MDL)

Occam's razor favors simple solutions over complex ones. Given some programming language, the principle of *Minimum Description Length* (MDL) can be used to measure the complexity of a solution candidate by the length of the shortest program that computes it, e.g., (Solomonoff, 1964; Kolmogorov, 1965b; Chaitin, 1966; Wallace and Boulton, 1968; Levin, 1973a; Rissanen, 1986; Li and Vitányi, 1997; Grünwald et al., 2005). Some methods explicitly take into account program runtime (Allender, 1992; Watanabe, 1992; Schmidhuber, 2002, 1995); many consider only programs with constant runtime, e.g., (Rissanen, 1986; Hinton and van Camp, 1993; Li and Vitányi, 1997).

In the NN case, the MDL principle suggests that low NN weight complexity corresponds to high NN probability in the Bayesian view, e.g., (MacKay, 1992; Buntine and Weigend, 1991), and high generalization performance, without overfitting the training data. Many methods have been proposed for *regularizing* NNs, that is, searching for solution-computing, low-complexity SL NNs (Sec. 5.6.3) and RL NNs (Sec. 6.7). This is closely related to certain UL methods (Sec. 4.2, 5.6.4).

4.4 Learning Hierarchical Representations in Deep SL, UL, RL

Many methods of *Good Old-Fashioned Artificial Intelligence* (GOFAI) (Nilsson, 1980) and more recent approaches to AI (Russell et al., 1995) learn hierarchies of more and more abstract data representations. For example, certain methods of syntactic pattern recognition (Fu, 1977) such as *grammar induction* discover hierarchies of formal rules to model observations. The partially (un)supervised *Automated Mathematician / EURISKO* (Lenat, 1983; Lenat and Brown, 1984) continually learns concepts by combining previously learnt concepts. Such hierarchical representation learning (Ring, 1994; Bengio et al., 2013; Deng and Yu, 2014) is also a recurring theme of DL NNs for SL (Sec. 5), UL-aided SL (Sec. 5.7, 5.9, 5.14), and hierarchical RL (Sec. 6.5). Often, abstract hierarchical representations are natural by-products of data compression (Sec. 4.3), e.g., (Sec. 5.9).

4.5 Fast GPU Hardware for DL NN

While the previous millennium saw several attempts at creating fast NN-specific hardware, e.g., (Jackel et al., 1990; Faggin, 1992; Ramacher et al., 1993; Widrow et al., 1994; Heemskerk, 1995; Korkin et al., 1997; Urlbe, 1999), the new millennium enabled a DL NN breakthrough in form of cheap, multi-processor graphics cards or GPUs. GPUs are widely used for video games, a huge and competitive market that drove down hardware prices. GPUs excel at fast matrix and vector multiplications required not only for convincing virtual realities but also for NN training, where they can speed up learning by a factor of 50 and more. Some of the GPU-based FNN implementations (Sec. 5.14 - 5.17) have greatly contributed to recent successes in contests for pattern recognition (Sec. 5.17 - 5.20), image segmentation (Sec. 5.19), and object detection (Sec. 5.19 - 5.20).

5 Supervised NNs, Some Helped by Unsupervised NNs

The main focus of current practical applications is on *Supervised Learning* (SL), which has dominated recent pattern recognition contests (Sec. 5.15-5.20). Several methods, however, use additional *Unsupervised Learning* (UL) to facilitate SL (Sec. 5.7, 5.9, 5.14). It does make sense to treat SL and UL in the same section: often gradient-based methods, such as BP (Sec. 5.4.1), are used to optimize objective functions of both UL and SL, and the boundary between SL and UL may blur, for example, when it comes to time series prediction and sequence classification, e.g., Sec. 5.9, 5.10.

A historical timeline format will help to arrange subsections on important inspirations and technical contributions (although such a subsection may span a time interval of many years). Sec. 5.1 briefly mentions early, shallow NN models since the 1940s, Sec. 5.2 additional early neurobiological inspiration relevant for modern Deep Learning (DL). Sec. 5.3 is about the relatively deep *Neocognitron* NN (1979) which is similar to certain modern deep FNN architectures, as it combines convolutional NNs (CNNs), weight pattern replication, and winner-take-all (WTA) mechanisms. Sec. 5.4 uses the notation of Sec. 2 to compactly describe a central algorithm of DL, namely, *backpropagation* (BP) for supervised weight-sharing FNNs and RNNs. It also summarizes the history of BP 1960-1981 and beyond. Sec. 5.5 is about applying BP to CNNs, important in today's DL applications. Sec. 5.6 describes problems encountered in the late 1980s with BP for deep NNs, and mentions several ideas from the previous millennium to overcome them; Sec. 5.7 mentions a first hierarchical stack of coupled UL-based Autoencoders (AEs). Sec. 5.8 explains BP's *Fundamental DL Problem* (of vanishing/exploding gradients) discovered in 1991. Sec. 5.9 explains how a deep RNN stack of 1991 (the *History Compressor*) pre-trained by UL helped to solve previously unlearnable DL benchmarks requiring *Credit Assignment Paths* (CAPs, Sec. 3) of depth 1000 and more. Sec. 5.10 mentions a first important contest won by SL NNs in 1994. Sec. 5.11 describes a purely supervised DL RNN (*Long Short-Term Memory*, LSTM) for problems of depth 1000 and more. Sec. 5.12 mentions a particular WTA method called *Max-Pooling* (MP) important in today's DL FNNs. Sec. 5.13 mentions an early contest of 2003 won by an ensemble of shallow NNs, as well as good pattern recognition results with CNNs (2003) and LSTM RNNs. Sec. 5.14 is mostly about *Deep Belief Networks* (DBNs, 2006) and related stacks of *Autoencoders* (AEs, Sec. 5.7) pre-trained by UL to facilitate SL. Sec. 5.15-5.20 focus on official competitions with secret test sets won by DL NNs since 2009, in sequence recognition, image classification, image segmentation, and object detection. Many RNN results depended on LSTM (Sec. 5.11); many FNN results depended on GPU-based FNN code developed since 2004 (Sec. 5.14, 5.15, 5.16, 5.17), in particular, GPU-MPCNNs (Sec. 5.17).

5.1 1940s and Earlier

NN research started in the 1940s, e.g., (McCulloch and Pitts, 1943; Hebb, 1949); compare also later work (Rosenblatt, 1958, 1962; Widrow and Hoff, 1962; Grossberg, 1969; Kohonen, 1972; von der Malsburg, 1973; Narendra and Thathatchar, 1974; Willshaw and von der Malsburg, 1976; Palm, 1980; Hopfield, 1982). In a sense NNs have been around even longer, since early supervised NNs were essentially variants of linear regression methods going back at least to the early 1800s, e.g., (Gauss, 1821). Early NNs had a maximal CAP depth of 1 (Sec. 3).

5.2 Around 1960: More Neurobiological Inspiration for DL

Simple cells and complex cells were found in the visual cortex, e.g., (Hubel and Wiesel, 1962; Wiesel and Hubel, 1959). These cells fire in response to certain properties of visual sensory inputs, such as the orientation of edges. Complex cells exhibit more spatial invariance than simple cells. This inspired later deep NN architectures (Sec. 5.3) used in certain modern award-winning Deep Learners (Sec. 5.17-5.20).

5.3 1979: Convolution + Weight Replication + Winner-Take-All (WTA)

The *Neocognitron* (Fukushima, 1979, 1980, 2013a) was perhaps the first artificial NN that deserved the attribute *deep*, and the first to incorporate the neurophysiological insights of Sec. 5.2. It introduced *convolutional NNs* (today often called CNNs or convnets), where the (typically rectangular) receptive field

of a *convolutional unit* with given weight vector is shifted step by step across a 2-dimensional array of input values, such as the pixels of an image. The resulting 2D array of subsequent activation events of this unit can then provide inputs to higher-level units, and so on. Due to massive *weight replication* (Sec. 2), relatively few parameters may be necessary to describe the behavior of such a *convolutional layer*.

Competition layers have WTA subsets whose maximally active units are the only ones to adopt non-zero activation values. They essentially “down-sample” the competition layer’s input. This helps to create units whose responses are insensitive to small image shifts (compare Sec. 5.2).

The Neocognitron is very similar to the architecture of modern, contest-winning, purely *supervised*, feedforward, gradient-based Deep Learners with alternating convolutional and competition layers (Sec. 5.17-5.20). Fukushima, however, did not set the weights by supervised backpropagation (Sec. 5.4, 5.5), but by local *unsupervised* learning rules, e.g., (Fukushima, 2013b), or by pre-wiring. In that sense he did not care for the DL problem (Sec. 5.8), although his architecture was comparatively deep indeed. He also used spatial averaging (Fukushima, 1980, 2011) instead of max-pooling (MP, Sec. 5.12), today a particularly convenient and popular WTA mechanism. Today’s CNN-based DL machines profit a lot from later CNN work, e.g., (LeCun et al., 1989; Ranzato et al., 2007) (Sec. 5.5, 5.14, 5.17).

5.4 1960-1981 and Beyond: Development of Backpropagation (BP) for NNs

The minimisation of errors through gradient descent (Hadamard, 1908) in the parameter space of complex, nonlinear, multi-stage, differentiable, NN-related systems has been discussed at least since the early 1960s, e.g., (Kelley, 1960; Bryson, 1961; Bryson and Denham, 1961; Pontryagin et al., 1961; Dreyfus, 1962; Wilkinson, 1965; Amari, 1967; Bryson and Ho, 1969; Director and Rohrer, 1969; Griewank, 2012), initially within the framework of Euler-LaGrange equations in the *Calculus of Variations*, e.g., (Euler, 1744). Steepest descent in such systems can be performed (Bryson, 1961; Kelley, 1960; Bryson and Ho, 1969) by iterating the ancient chain rule (Leibniz, 1676; L’Hôpital, 1696) in *Dynamic Programming* (DP) style (Bellman, 1957). A simplified derivation uses the chain rule only (Dreyfus, 1962). The systems of the 1960s were already efficient in the DP sense. However, they backpropagated derivative information through standard Jacobian matrix calculations from one “layer” to the previous one, explicitly addressing neither direct links across several layers nor potential additional efficiency gains due to network sparsity (but perhaps such enhancements seemed obvious to the authors).

Explicit, efficient error backpropagation (BP) in arbitrary, discrete, possibly sparsely connected, NN-like networks apparently was first described in 1970 (Linnainmaa, 1970, 1976), albeit without reference to NNs. BP is also known as the reverse mode of automatic differentiation (Griewank, 2012), where the costs of forward activation spreading essentially equal the costs of backward derivative calculation. See early FORTRAN code (Linnainmaa, 1970); see also (Ostrovskii et al., 1971). Efficient BP was soon explicitly used to minimize cost functions by adapting control parameters (weights) (Dreyfus, 1973). Compare some NN-specific discussion (Werbos, 1974, section 5.5.1), a method for multilayer threshold NNs (Bobrowski, 1978), and a computer program for automatically deriving and implementing BP for given differentiable systems (Speelpenning, 1980).

To my knowledge, the first NN-specific application of efficient BP was described in 1981 (Werbos, 1981, 2006). See also (LeCun, 1985; Parker, 1985; LeCun, 1988). A paper of 1986 significantly contributed to the popularisation of BP (Rumelhart et al., 1986). See generalisations for sequence-processing recurrent NNs, e.g., (Williams, 1989; Robinson and Fallside, 1987; Werbos, 1988; Williams and Zipser, 1988, 1989b,a; Rohwer, 1989; Pearlmutter, 1989; Gherrity, 1989; Williams and Peng, 1990; Schmidhuber, 1992a; Pearlmutter, 1995; Kremer and Kolen, 2001; Atiya and Parlos, 2000), also for equilibrium RNNs (Almeida, 1987; Pineda, 1987) with stationary inputs. See also natural gradients (Amari, 1998).

5.4.1 BP for Weight-Sharing FNNs and RNNs

Using the notation of Sec. 2 for weight-sharing FNNs or RNNs, after an episode of activation spreading through differentiable f_t , a single iteration of gradient descent through BP computes changes of all w_i in proportion to $\frac{\partial E}{\partial w_i} = \sum_t \frac{\partial E}{\partial net_t} \frac{\partial net_t}{\partial w_i}$ as in Algorithm 5.4.1 (for the additive case), where each weight w_i is associated with a real-valued variable Δ_i initialized by 0.

Alg. 5.4.1: One iteration of BP for weight-sharing FNNs or RNNs

```
for  $t = T, \dots, 1$  do
  to compute  $\frac{\partial E}{\partial net_t}$ , initialize real-valued error signal variable  $\delta_t$  by 0;
  if  $x_t$  is an input event then continue with next iteration;
  if there is an error  $e_t$  then  $\delta_t := x_t - d_t$ ;
  add to  $\delta_t$  the value  $\sum_{k \in out_t} w_{v(t,k)} \delta_k$ ; (this is the elegant and efficient recursive chain rule application
  collecting impacts of  $net_t$  on future events)
  multiply  $\delta_t$  by  $f'_t(net_t)$ ;
  for all  $k \in in_t$  add to  $\Delta_{w_{v(k,t)}}$  the value  $x_k \delta_t$ 
end for
```

Finally, to finish one iteration of steepest descent, change all w_i in proportion to Δ_i and a small learning rate. The computational costs of the backward (BP) pass are essentially those of the forward pass (Sec. 2). Forward and backward passes are re-iterated until sufficient performance is reached.

As of 2013, this simple BP method is still the central learning algorithm for FNNs and RNNs. Notably, most contest-winning NNs up to 2013 (Sec. 5.10, 5.13, 5.15, 5.17, 5.19, 5.20) did *not* augment supervised BP by some sort of *unsupervised* learning as discussed in Sec. 5.7, 5.9, 5.14.

5.5 1989: BP for CNNs

In 1989, backpropagation (Sec. 5.4) was applied (LeCun et al., 1989, 1990a, 1998) to weight-sharing convolutional neural layers with adaptive connections (compare Sec. 5.3). This combination, augmented by max-pooling (Sec. 5.12), and sped up on graphics cards (Sec. 5.17), has become an essential ingredient of many modern, competition-winning, feedforward, visual Deep Learners (Sec. 5.17-5.19). This work also introduced the MNIST data set of handwritten digits (LeCun et al., 1989), which over time has become perhaps the most famous benchmark of Machine Learning. A CNN of depth 5 achieved good performance on MNIST (LeCun et al., 1990a); similar CNNs were used commercially in the 1990s.

5.6 Late 1980s-2000: Improvements of NNs

By the late 1980s it seemed clear that BP by itself (Sec. 5.4) was no panacea. Most FNN applications focused on FNNs with few hidden layers. Many practitioners found solace in a theorem (Kolmogorov, 1965a) stating that an NN with a single layer of enough hidden units can approximate any multivariate continuous function with arbitrary accuracy. Additional hidden layers often did not seem to offer empirical benefits.

Likewise, most RNN applications did not require backpropagating errors far. Many researchers helped their RNNs by first training them on shallow problems (Sec. 3) whose solutions then generalized to deeper problems. In fact, some popular RNN algorithms restricted credit assignment to a single step backwards (Elman, 1988; Jordan, 1986), also in more recent studies (Jaeger, 2002; Maass et al., 2002; Jaeger, 2004).

Generally speaking, although BP allows for deep problems in principle, it seemed to work only for *shallow* problems. The late 1980s and early 1990s saw a few ideas with a potential to overcome this problem, which was fully understood only in 1991 (Sec. 5.8).

5.6.1 Ideas for Dealing with Long Time Lags and Deep CAPs

To deal with long time lags between relevant events, several sequence processing methods were proposed, including *focused BP* for RNNs (Mozier, 1989, 1992), *Time-Delay Neural Networks* (Lang et al., 1990) and their adaptive extension (Bodenhausen and Waibel, 1991), *NARX RNNs* (Lin et al., 1995, 1996), certain hierarchical RNNs (Hihi and Bengio, 1996), RL economies in RNNs with WTA units (Schmidhuber, 1989b), and other methods, e.g., (Ring, 1993, 1994; Plate, 1993; de Vries and Principe, 1991; Sun et al., 1993a; Bengio et al., 1994). However, these algorithms either worked for shallow CAPs only, could not generalize to unseen CAP depths, had problems with greatly varying time lags between relevant events,

needed external fine tuning of delay constants, or suffered from other problems. In fact, it turned out that certain simple but deep benchmark problems used to evaluate such methods are more quickly solved by randomly guessing RNN weights until a solution is found (Hochreiter and Schmidhuber, 1996).

While the methods above were designed for DL in RNNs, the *Neural Heat Exchanger* (Schmidhuber, 1990c) consists of two parallel *deep FNNs* with opposite flow directions. Input patterns enter the first FNN and are propagated “up”. Desired outputs (targets) enter the “opposite” FNN and are propagated “down”. Using a local learning rule, each layer in each net tries to be similar (in information content) to the preceding layer and to the adjacent layer of the other net. The input entering the first net slowly “heats up” to become the target. The target entering the opposite net slowly “cools down” to become the input. The *Helmholtz Machine* (Dayan et al., 1995; Dayan and Hinton, 1996) may be viewed as an unsupervised (Sec. 5.6.4) variant thereof (Peter Dayan, personal communication, 1994).

5.6.2 Better BP Through Advanced Gradient Descent

Numerous improvements of steepest descent through BP (Sec. 5.4) have been proposed. Least-squares methods (Gauss-Newton, Levenberg-Marquardt) (Levenberg, 1944; Marquardt, 1963) and quasi-Newton methods (Broyden-Fletcher-Goldfarb-Shanno, BFGS) (Broyden et al., 1965; Fletcher and Powell, 1963; Goldfarb, 1970; Shanno, 1970) are computationally too expensive for large NNs. Partial BFGS (Battiti, 1992; Saito and Nakano, 1997) and conjugate gradient (Hestenes and Stiefel, 1952; Møller, 1993) as well as other methods (Solla, 1988; Schmidhuber, 1989a; Cauwenberghs, 1993) provide sometimes useful fast alternatives. To speed up BP, *momentum* was introduced (Rumelhart et al., 1986), ad-hoc constants were added to the slope of the linearized activation function (Fahlman, 1988), or the nonlinearity of the slope was exaggerated (West and Saad, 1995). Only the signs of the error derivatives are taken into account by the successful and widely used BP variant *R-prop* (Riedmiller and Braun, 1993). The local gradient can be normalized based on the NN architecture (Schraudolph and Sejnowski, 1996), through a diagonalized Hessian approach (Becker and Le Cun, 1989), or related efficient methods (Schraudolph, 2002). BP can be treated as a linear least-squares problem (Biegler-König and Bärman, 1993), where second-order gradient information is passed back to preceding layers. Some algorithms for controlling BP step size adapt a global learning rate (Lapedes and Farber, 1986; Vogl et al., 1988; Battiti, 1989; LeCun et al., 1993; Yu et al., 1995), others compute individual learning rates for each weight (Jacobs, 1988; Silva and Almeida, 1990). In online learning, where BP is applied after each pattern presentation, the *vario- η* algorithm (Neuneier and Zimmermann, 1996) sets each weight’s learning rate inversely proportional to the empirical standard deviation of its local gradient, thus normalizing the stochastic weight fluctuations. Compare a local online step size adaptation method for nonlinear NNs (Almeida et al., 1997). Many additional tricks for improving NNs have been described, e.g., (Orr and Müller, 1998; Montavon et al., 2012). Compare Sec. 5.6.3 and recent developments mentioned in Sec. 5.21.

5.6.3 Discovering Low-Complexity, Problem-Solving NNs

Many researchers used BP-like methods to search for low-complexity NNs (Sec. 4.3) with high generalization capability. Most approaches address the *bias/variance dilemma* (Geman et al., 1992) through strong prior assumptions. For example, *weight decay* (Hanson and Pratt, 1989; Weigend et al., 1991; Krogh and Hertz, 1992) prefers small weights and can be derived from Gaussian or Laplace weight priors (Hinton and van Camp, 1993); see also (Murray and Edwards, 1993). Some assume that a distribution of networks with many similar weights generated by Gaussian mixtures is “better” *a priori* (Nowlan and Hinton, 1992). Other weight priors are implicit in additional penalty terms (MacKay, 1992) or in methods based on *validation sets* (Mosteller and Tukey, 1968; Stone, 1974; Eubank, 1988; Hastie and Tibshirani, 1990; Craven and Wahba, 1979; Golub et al., 1979), *final prediction error* (Akaike, 1970), *generalized prediction error* (Moody and Utans, 1994; Moody, 1992); see also (Holden, 1994; Wang et al., 1994; Amari and Murata, 1993; Wang et al., 1994; Guyon et al., 1992; Vapnik, 1992; Wolpert, 1994). Similar priors are implicit in constructive and pruning algorithms, e.g., *sequential network construction* (Fahlman, 1991; Ash, 1989; Moody, 1989), *input pruning* (Moody, 1992; Nicholas Refenes et al., 1994), *unit pruning* (White, 1989; Mozer and Smolensky, 1989; Levin et al., 1994), *weight pruning*, e.g., *optimal brain damage* (LeCun et al., 1990b), and *optimal brain surgeon* (Hassibi and Stork, 1993). A very general but not always practical

approach for discovering low-complexity SL NNs or RL NNs searches among weight matrix-computing programs written in a universal programming language (Schmidhuber, 1995, 1997) (Sec. 6.7). *Flat Minimum Search* (FMS) (Hochreiter and Schmidhuber, 1997a, 1999) searches for a “flat” minimum of the error function: a large connected region in weight space where error is low and remains approximately constant, that is, few bits of information are required to describe low-precision weights with high variance. Compare *perturbation tolerance conditions* (Minai and Williams, 1994; Murray and Edwards, 1993; Neti et al., 1992; Matsuoka, 1992; Bishop, 1993; Kerlirzin and Vallet, 1993; Carter et al., 1990). An MDL-based, Bayesian argument suggests that flat minima correspond to “simple” NNs and low expected overfitting. Compare Sec. 5.6.4 and more recent developments mentioned in Sec. 5.21.

5.6.4 Potential Benefits of UL for SL

The SL notation of Sec. 2 focused on teacher-given labels d_t . Many papers of the previous millennium, however, were about *unsupervised learning (UL) without a teacher*, e.g., (Hebb, 1949; von der Malsburg, 1973; Kohonen, 1972, 1982, 1988; Willshaw and von der Malsburg, 1976; Grossberg, 1976a,b; Watanabe, 1985; Pearlmutter and Hinton, 1986; Barrow, 1987; Field, 1987; Oja, 1989; Barlow et al., 1989; Baldi and Hornik, 1989; Rubner and Tavan, 1989; Sanger, 1989; Ritter and Kohonen, 1989; Rubner and Schulten, 1990; Földiák, 1990; Martinetz et al., 1990; Kosko, 1990; Mozer, 1991; Palm, 1992; Atick et al., 1992; Schmidhuber and Prelinger, 1993; Miller, 1994; Saund, 1994; Földiák and Young, 1995; Deco and Parra, 1997); see also post-2000 work, e.g., (Klapper-Rybicka et al., 2001; Wiskott and Sejnowski, 2002; Franzius et al., 2007; Waydo and Koch, 2008). Many UL methods are designed to maximize information-theoretic objectives, e.g., (Linsker, 1988; Barlow et al., 1989; MacKay and Miller, 1990; Becker, 1990; Plumbley, 1991; Schmidhuber, 1992b,c; Schraudolph and Sejnowski, 1993; Redlich, 1993; Zemel, 1993; Zemel and Hinton, 1994; Field, 1994; Hinton et al., 1995; Dayan and Zemel, 1995; Amari et al., 1996; Deco and Parra, 1997), and to uncover and disentangle hidden underlying sources of signals, e.g., (Jutten and Herault, 1991; Schuster, 1992; Andrade et al., 1993; Molgedey and Schuster, 1994; Comon, 1994; Cardoso, 1994; Bell and Sejnowski, 1995; Belouchrani et al., 1997; Hyvärinen and Oja, 2000). Many UL methods automatically and robustly generate distributed, sparse representations of input patterns (Földiák, 1990; Olshausen and Field, 1996; Hinton and Ghahramani, 1997; Lewicki and Olshausen, 1998; Hyvarinen et al., 1999; Hochreiter and Schmidhuber, 1999) through well-known feature detectors, such as orientation sensitive edge detectors and off-center-on-surround-like structures, e.g., (Olshausen and Field, 1996; Schmidhuber et al., 1996), thus extracting simple features related to those considered useful for image pre-processing and compression, and also to those observed in early visual pre-processing stages of biological systems.

UL can help to encode input data in a form advantageous for further processing. In the context of DL, one important goal of UL is redundancy reduction. Ideally, given an ensemble of input patterns, redundancy reduction through a deep NN will create a *factorial code* (a code with statistically independent components) of the ensemble (Barlow et al., 1989; Barlow, 1989), to disentangle the unknown factors of variation, e.g., (Bengio et al., 2013). Such codes may be sparse and can be advantageous for (1) data compression, (2) speeding up subsequent BP (Becker, 1991), (3) trivialising the task of subsequent naive yet optimal Bayes classifiers (Schmidhuber et al., 1996).

Most early UL FNNs had a single layer. Methods for deeper FNNs include nonlinear *Autoencoders* (AEs) with more than 3 (e.g., 5) layers (Kramer, 1991; Oja, 1991; DeMers and Cottrell, 1993). Such an AE NN (Rumelhart et al., 1986) can be trained to map input patterns to themselves, for example, by compactly encoding them through activations of units of a narrow bottleneck hidden layer. Other non-linear methods include *Predictability Minimization* (PM) (Schmidhuber, 1992c), where non-linear feature detectors fight non-linear predictors, trying to become both informative and as unpredictable as possible, and *LOCOCODE* (Hochreiter and Schmidhuber, 1999), where FMS (Sec. 5.6.3) is applied to find low-complexity AEs with low-precision weights describable by few bits of information, often yielding sparse or factorial codes.

5.7 1987: UL Through Autoencoder (AE) Hierarchies

Perhaps the first work to study potential benefits of UL-based pre-training was published in 1987. It proposed unsupervised AE hierarchies (Ballard, 1987), closely related to certain post-2000 feedforward

Deep Learners based on UL (Sec. 5.14). The lowest-level AE NN with a single hidden layer is trained to map input patterns to themselves. Its hidden layer codes are then fed into a higher-level AE of the same type, and so on. The hope is that the codes in the hidden AE layers have properties that facilitate subsequent learning. In one experiment, a particular AE-specific learning algorithm (different from traditional BP of Sec. 5.4.1) was used to learn a mapping in an AE stack pre-trained by this type of UL (Ballard, 1987). This was faster than learning an equivalent mapping by BP through a single deeper AE without pre-training. On the other hand, the task did not really require a deep AE, that is, the benefits of UL were not that obvious from this experiment. Compare an early survey (Hinton, 1989) and the somewhat related *Recursive Auto-Associative Memory* (RAAM) (Pollack, 1988, 1990; Melnik et al., 2000), originally used to encode linguistic structures, but later also as an unsupervised pre-processor to facilitate deep credit assignment for RL (Gisslen et al., 2011) (Sec. 6.4).

In principle, many UL methods (Sec. 5.6.4) could be stacked like the AEs above, the RNNs of Sec. 5.9, or the Deep Belief Nets of Sec. 5.9, to facilitate subsequent SL. Compare *Stacked Generalization* (Wolpert, 1992).

5.8 1991: Fundamental Deep Learning Problem of Gradient Descent

A diploma thesis (Hochreiter, 1991) represented a milestone of explicit DL research. As mentioned in Sec. 5.6, by the late 1980s, experiments had indicated that traditional deep feedforward or recurrent networks are hard to train by backpropagation (BP) (Sec. 5.4). Hochreiter's work formally identified a major reason: Typical deep NNs suffer from the now famous problem of vanishing or exploding gradients. With standard activation functions (Sec. 1), cumulative backpropagated error signals (Sec. 5.4.1) either shrink rapidly, or grow out of bounds. In fact, they decay exponentially in the number of layers or CAP depth (Sec. 3), or they explode. This is also known as the *long time lag problem*. Much subsequent DL research of the 1990s and 2000s was motivated by this insight. Compare (Bengio et al., 1994), who also studied basins of attraction and their stability under noise from a dynamical systems point of view: either the dynamics are not robust to noise, or the gradients vanish; see also (Hochreiter et al., 2001a; Tiño and Hammer, 2004). Over the years, several ways of partially overcoming the *Fundamental Deep Learning Problem* were explored:

- I A Very Deep Learner of 1991 (Sec. 5.9) alleviates the problem through unsupervised pre-training for a hierarchy of RNNs. This greatly facilitates subsequent supervised credit assignment through BP (Sec. 5.4). Compare conceptually related AE stacks (Sec. 5.7) and Deep Belief Nets (Sec. 5.14) for the FNN case.
- II LSTM-like networks (Sec. 5.11, 5.15, 5.20) alleviate the problem through a special architecture unaffected by it.
- III Today's GPU-based computers have a million times the computational power of desktop machines of the early 1990s. This allows for propagating errors a few layers further down within reasonable time, even in traditional NNs (Sec. 5.16). That is basically what is winning many of the image recognition competitions now (Sec. 5.17, 5.19, 5.20). (Although this does not really overcome the problem in a fundamental way.)
- IV Hessian-free optimization (Sec. 5.6.2) can alleviate the problem for FNNs (Møller, 1993; Pearlmutter, 1994; Schraudolph, 2002; Martens, 2010) (Sec. 5.6.2) and RNNs (Martens and Sutskever, 2011) (Sec. 5.18).
- V The space of NN weight matrices can also be searched without relying on error gradients, thus avoiding the *Fundamental Deep Learning Problem* altogether. Random weight guessing sometimes works better than more sophisticated methods (Hochreiter and Schmidhuber, 1996). Certain more complex problems are better solved by using *Universal Search* (Levin, 1973b) for weight matrix-computing programs written in a universal programming language (Schmidhuber, 1995, 1997). Some are better solved by using linear methods to obtain optimal weights for connections to output events, and evolving weights of connections to other events—this is called *Evolino* (Schmidhuber et al., 2007);

compare related RNNs pre-trained by certain UL rules (Steil, 2007). Direct search methods are relevant not only for SL but also for more general RL, and are discussed in more detail in Sec. 6.6.

5.9 1991-: Deep Hierarchy of Recurrent NNs

A working *Very Deep Learner* (Sec. 3) of 1991 (Schmidhuber, 1992b, 2013a) could perform credit assignment across hundreds of nonlinear operators or neural layers, by using *unsupervised pre-training* for a stack of RNNs.

The basic idea is still relevant today. Each RNN is trained for a while in unsupervised fashion to predict its next input; e.g., (Connor et al., 1994; Dorffner, 1996). From then on, only unexpected inputs (errors) convey new information and get fed to the next higher RNN which thus ticks on a slower, self-organising time scale. It can easily be shown that no information gets lost. It just gets compressed (much of machine learning is essentially about compression, e.g., Sec. 4.3, 5.6.3, 6.7). For each individual input sequence, we get a series of less and less redundant encodings in deeper and deeper levels of this *History Compressor*, which can compress data in both space (like feedforward NNs) and time. There also is a continuous variant (Schmidhuber et al., 1993).

The RNN stack is essentially a deep generative model of the data, which can be reconstructed from its compressed form. Adding another RNN to the stack improves a bound on the data’s description length—equivalent to the negative logarithm of its probability (Huffman, 1952; Shannon, 1948)—as long as there is remaining local learnable predictability in the data representation on the corresponding level of the hierarchy.

The system was able to learn many previously unlearnable DL tasks. One ancient illustrative DL experiment (Schmidhuber, 1993b) required CAPs (Sec. 3) of depth 1200. The top level code of the initially unsupervised RNN stack, however, got so compact that (previously infeasible) sequence classification through additional SL became possible. Essentially the system used UL to greatly reduce CAP depth.

There is a way of compressing higher levels down into lower levels, thus fully or partially collapsing the RNN stack. The trick is to retrain a lower-level RNN to continually imitate (predict) the hidden units of an already trained, slower, higher-level RNN (the “conscious” chunker), through additional predictive output neurons (Schmidhuber, 1992b). This helps the lower RNN (the “automatizer”) to develop appropriate, rarely changing memories that may bridge very long time lags. Again, this procedure can greatly reduce the required depth of the BP process.

The 1991 system was a working Deep Learner in the modern post-2000 sense, and also a first *Neural Hierarchical Temporal Memory* (HTM). It is conceptually similar to AE hierarchies (Sec. 5.7) and later *Deep Belief Networks* (Sec. 5.14), but more general in the sense that it uses sequence-processing RNNs instead of FNNs with unchanging inputs. More recently, well-known entrepreneurs (Hawkins and George, 2006; Kurzweil, 2012) also got interested in HTMs. Stacks of RNNs were used in later work with great success, e.g., Sec. 5.11, 5.15, 5.20. Clockwork RNNs (Koutník et al., 2014) also consist of interacting RNN modules with different clock rates, but do not require UL to set those rates.

5.10 1994: Contest-Winning Not So Deep NNs

Back in the 1990s, certain NNs already won certain controlled pattern recognition contests with secret test sets. Notably, an NN with internal delay lines won the Santa Fe time-series competition on chaotic intensity pulsations of an NH₃ laser (Wan, 1994; Weigend and Gershenfeld, 1993). No very deep CAPs (Sec. 3) were needed though.

5.11 1995-: Supervised Deep Recurrent Learner (LSTM RNN)

Supervised *Long Short-Term Memory* (LSTM) RNN (Hochreiter and Schmidhuber, 1997b; Gers et al., 2000; Pérez-Ortiz et al., 2003) could eventually perform similar feats as the deep RNN hierarchy of 1991 (Sec. 5.9), overcoming the *Fundamental Deep Learning Problem* (Sec. 5.8) without any unsupervised pre-training. LSTM could also learn DL tasks *without* local sequence predictability (and thus *unlearnable* by the partially unsupervised 1991 History Compressor, Sec. 5.9), dealing with CAPs (Sec. 3) of depth 1000 and more, e.g., (Gers and Schmidhuber, 2001; Gers et al., 2002).

The basic LSTM idea is very simple. Some of the units are called constant error carrousel (CECs). Each CEC uses as an activation function f , the identity function, and has a connection to itself with fixed weight of 1.0. Due to f 's constant derivative of 1.0, errors backpropagated through a CEC cannot vanish or explode but stay as they are (unless they “flow out” of the CEC to other units). This is the main reason why LSTM nets can learn to discover the importance of (and memorize) events that happened thousands of discrete time steps ago, while previous RNNs already failed in case of minimal time lags of 10 steps. Some LSTM variants also use *modifiable* self-connections of CECs (Gers and Schmidhuber, 2001).

A CEC is connected to several *nonlinear* adaptive units (often including multiplicative gates) needed for learning nonlinear behavior (often using error signals propagated far back in time through a CEC). Many different LSTM variants and topologies are allowed. It is possible to evolve good problem-specific topologies (Bayer et al., 2009). Compare also more recent RNN algorithms able to deal with long time lags (Schäfer et al., 2006; Martens and Sutskever, 2011; Zimmermann et al., 2012; Koutník et al., 2014).

To a certain extent, LSTM is biologically plausible (O’Reilly, 2003). LSTM learned to solve many previously unlearnable DL tasks involving: Recognition of the temporal order of widely separated events in noisy input streams; Robust storage of high-precision real numbers across extended time intervals; Arithmetic operations on continuous input streams; Extraction of information conveyed by the temporal distance between events; Recognition of temporally extended patterns in noisy input sequences (Hochreiter and Schmidhuber, 1997b; Gers et al., 2000); Stable generation of precisely timed rhythms (Gers and Schmidhuber, 2000), smooth and non-smooth periodic trajectories. LSTM clearly outperformed previous RNNs on tasks that require learning the rules of regular languages describable by deterministic *Finite State Automata* (FSAs) (Watrous and Kuhn, 1992; Casey, 1996; Siegelmann, 1992; Blair and Pollack, 1997; Kalinke and Lehmann, 1998; Zeng et al., 1994; Manolios and Fanelli, 1994; Omlin and Giles, 1996; Vahed and Omlin, 2004), both in terms of reliability and speed. LSTM also worked better on tasks involving context free languages (CFLs) that cannot be represented by HMMs or similar FSAs discussed in the RNN literature (Sun et al., 1993b; Wiles and Elman, 1995; Andrews et al., 1995; Steijvers and Grunwald, 1996; Tonkes and Wiles, 1997; Rodriguez et al., 1999; Rodriguez and Wiles, 1998). CFL recognition (Lee, 1996) requires the functional equivalent of a stack. Some previous RNNs failed to learn small CFL training sets (Rodriguez and Wiles, 1998). Those that did not (Rodriguez et al., 1999; Bodén and Wiles, 2000) failed to extract the general rules, and did not generalize well on substantially larger test sets. Similar for context-sensitive languages (CSLs), e.g., (Chalup and Blair, 2003). LSTM generalized well though, requiring only the 30 shortest exemplars ($n \leq 10$) of the CSL $a^n b^n c^n$ to correctly predict the possible continuations of sequence prefixes for n up to 1000 and more. A combination of a decoupled extended Kalman filter (Puskorius and Feldkamp, 1994) and an LSTM RNN (Pérez-Ortiz et al., 2003) learned to deal correctly with values of n up to 10 million and more. That is, after training the network was able to read sequences of 30,000,000 symbols and more, one symbol at a time, and finally detect the subtle differences between *legal* strings such as $a^{10,000,000} b^{10,000,000} c^{10,000,000}$ and very similar but *illegal* strings such as $a^{10,000,000} b^{9,999,999} c^{10,000,000}$.

Bi-directional RNNs (Schuster and Paliwal, 1997; Schuster, 1999) are designed for input sequences whose starts and ends are known in advance, such as spoken sentences to be labeled by their phonemes; compare (Fukada et al., 1999; Baldi et al., 2001). To take both past and future context of each sequence element into account, one RNN processes the sequence from start to end, the other backwards from end to start. At each time step their combined outputs predict the corresponding label (if there is any). Bi-directional RNNs unfold their full potential when combined with the LSTM concept (Graves and Schmidhuber, 2005; Graves et al., 2009; Graves and Schmidhuber, 2009). DAG-RNNs (Baldi and Pollastri, 2003) generalize bi-directional RNNs to multiple dimensions.

Particularly successful in recent competitions are stacks (Sec. 5.9) of LSTM RNNs (Fernandez et al., 2007; Graves and Schmidhuber, 2009) trained by *Connectionist Temporal Classification* (CTC) (Graves et al., 2006), a gradient-based method for finding RNN weights that maximize the probability of teacher-given label sequences, given (typically much longer and more high-dimensional) streams of real-valued input vectors. CTC-LSTM performs simultaneous segmentation (alignment) and recognition (Sec. 5.20).

In the early 2000s, speech recognition was still dominated by HMMs combined with FNNs, e.g., (Bourlard and Morgan, 1994). Nevertheless, when trained from scratch on utterances from the TIDIGITS speech database, in 2003 LSTM already obtained results comparable to those of HMM-based systems (Graves et al., 2003; Beringer et al., 2005; Graves et al., 2006). In 2013, LSTM achieved best known results on the famous TIMIT phoneme recognition benchmark (Graves et al., 2013) (Sec. 5.20). Besides

speech recognition and keyword spotting (Fernández et al., 2007), important applications of LSTM include protein analysis (Hochreiter and Obermayer, 2005), robot localization (Förster et al., 2007) and robot control (Mayer et al., 2008), handwriting recognition (Graves et al., 2008, 2009; Graves and Schmidhuber, 2009; Bluche et al., 2014), optical character recognition (Breuel et al., 2013), and others. RNNs can also be used for metalearning (Schmidhuber, 1987; Schaul and Schmidhuber, 2010) because they can in principle learn to run their own weight change algorithm (Schmidhuber, 1993a). A successful metalearner (Hochreiter et al., 2001b) used an LSTM RNN to quickly *learn a learning algorithm* for quadratic functions (compare Sec. 6.8).

More recently, LSTM RNNs won several international pattern recognition competitions and set benchmark records on large and complex data sets, e.g., Sec. 5.15, 5.19, 5.20. LSTM is no panacea though—other RNNs sometimes outperformed LSTM at least on certain tasks (Jaeger, 2004; Martens and Sutskever, 2011; Pascanu et al., 2013b; Koutník et al., 2014) (compare Sec. 5.18).

5.12 1999: Max-Pooling (MP)

The feedforward HMAX model (Riesenhuber and Poggio, 1999) is similar to the Neocognitron (Sec. 5.3), but uses max-pooling layers instead of alternative local WTA methods, e.g., (Fukushima, 1980; Schmidhuber, 1989b; Maass, 2000; Fukushima, 2013a). Here a 2-dimensional layer or array of unit activations is partitioned into smaller rectangular arrays. Each is replaced in a down-sampling layer by the activation of its maximally active unit.

This is noteworthy because max-pooling (MP) CNNs or convnets (Sec. 5.3, 5.5) have become an essential ingredient of many modern, competition-winning, feedforward, visual Deep Learners (Sec. 5.17-5.19). Unlike HMAX, however, these are trained by BP (Sec. 5.4), which was applied to such MPCNNs only much later (Ranzato et al., 2007). Advantages of doing this were pointed out subsequently (Scherer et al., 2010).

5.13 2003: More Contest-Winning/Record-Setting, Often Not So Deep NNs

In the decade around 2000, many practical and commercial pattern recognition applications were dominated by non-neural machine learning methods such as *Support Vector Machines* (SVMs) (Vapnik, 1995; Schölkopf et al., 1998). Nevertheless, at least in certain domains, NNs outperformed other techniques.

A *Bayes NN* (Neal, 2006) based on an ensemble (Breiman, 1996) of NNs won the *NIPS 2003 Feature Selection Challenge* with secret test set (Neal and Zhang, 2006). The NN was not very deep though—it had two hidden layers and thus rather shallow CAPs (Sec. 3) of depth 3.

Important for many present competition-winning pattern recognisers (Sec. 5.17, 5.19, 5.20) were developments in the CNN department. A BP-trained (LeCun et al., 1989) CNN (Sec. 5.3, Sec. 5.5) set a new MNIST record of 0.4% (Simard et al., 2003), using training pattern deformations (Baird, 1990) but no unsupervised pre-training (Sec. 5.9, 5.14). A standard BP net achieved 0.7% (Simard et al., 2003). Again, the corresponding CAP depth was low. Compare further improvements in Sec. 5.14, 5.16, 5.17.

Good image interpretation results (Behnke, 2003) were achieved with rather deep NNs trained by the BP variant *R-prop* (Riedmiller and Braun, 1993) (Sec. 5.6.2).

Deep LSTM RNNs started to obtain certain first speech recognition results comparable to those of HMM-based systems (Graves et al., 2003); compare Sec. 5.11, 5.19, 5.20.

5.14 2006: Deep Belief Networks / Improved CNNs / GPU-CNNs

While explicit DL research results have been published at least since 1991 (Sec. 5.8, 5.9), the expression *Deep Learning* (DL) was actually coined relatively late, around 2006, in the context of unsupervised pre-training of NN (Hinton and Salakhutdinov, 2006; Hinton et al., 2006) for accelerating subsequent supervised learning through BP.

The *Deep Belief Network* (DBN) is a stack of *Restricted Boltzmann Machines* (RBMs) (Smolensky, 1986), which in turn are *Boltzmann Machines* (Hinton and Sejnowski, 1986) with a single layer of feature-detecting units. Each RBM perceives pattern representations from the level below and learns to encode

them in unsupervised fashion. At least in theory under certain assumptions, adding more layers improves a bound on the data’s negative log probability (equivalent to its description length—compare Sec. 5.9).

Without any training pattern deformations (Sec. 5.13), such a system (re-trained by supervised BP) achieved 1.2% error rate (Hinton and Salakhutdinov, 2006) on the MNIST handwritten digits (Sec. 5.5, 5.13). This result helped to arouse interest in deep NNs. DBNs also achieved good results on phoneme recognition (Mohamed et al., 2009; Mohamed and Hinton, 2010; Hinton et al., 2012a; Deng and Yu, 2014). Compare Sec. 5.20.

Autoencoder (AE) stacks (Ballard, 1987) (Sec. 5.7) became a popular alternative way of pre-training deep FNNs in unsupervised fashion before fine-tuning them through BP (Sec. 5.4) (Bengio et al., 2007; Erhan et al., 2010). Denoising AEs (Vincent et al., 2008) discourage hidden unit perturbations in response to input perturbations, similar to how FMS (Sec. 5.6.3) for LOCOCODE AEs (Sec. 5.6.4) discourages output perturbations in response to weight perturbations. Sparse coding (Sec. 5.6.4) was formulated as a combination of convex optimization problems (Lee et al., 2007a). A survey (Bengio, 2009) of stacked RBM and AE methods focuses on post-2006 developments.

Unsupervised DBNs and AE stacks are conceptually similar to, but in a sense less general than, the unsupervised RNN stack-based History Compressor of 1991 (Sec. 5.9), which can process not only stationary input patterns, but entire pattern sequences.

Also in 2006, a BP-trained (LeCun et al., 1989) CNN (Sec. 5.3, Sec. 5.5) set a new MNIST record of 0.39% (Ranzato et al., 2006), using training pattern deformations (Sec. 5.13) but no unsupervised pre-training. Compare further improvements in Sec. 5.16, 5.17. Similar CNNs were used for off-road obstacle avoidance (LeCun et al., 2006).

2006 also saw an early GPU-based CNN implementation (Chellapilla et al., 2006); compare earlier GPU-FNNs with a reported speed-up factor of 20 (Oh and Jung, 2004). GPUs or graphics cards have become more and more important for DL in subsequent years (Sec. 5.16-5.19).

5.15 2009: First Official Competitions Won by Deep Learning RNNs

Stacks (Sec. 5.9) of LSTM RNNs (Fernandez et al., 2007; Graves and Schmidhuber, 2009) trained by *Connectionist Temporal Classification* (CTC) (Graves et al., 2006) (Sec. 5.11) became the first RNNs to win official international pattern recognition contests (with secret test sets known only to the organisers). More precisely, three connected handwriting competitions at ICDAR 2009 in three different languages (French, Arab, Farsi) were won by deep LSTM RNNs without any *a priori* linguistic knowledge (Graves and Schmidhuber, 2009; Schmidhuber et al., 2011), performing simultaneous segmentation and recognition. Compare (Graves and Schmidhuber, 2005; Graves et al., 2006, 2009; Graves and Schmidhuber, 2009; Schmidhuber et al., 2011; Graves et al., 2013) (Sec. 5.20).

2009 also saw an impressive GPU-DBN implementation (Raina et al., 2009) orders of magnitudes faster than previous CPU-DBNs (see Sec. 5.14); see also (Coates et al., 2013).

5.16 2010: Plain Backprop (+ Distortions) on GPU Yields Excellent Results

In 2010, a new MNIST record of 0.35% error rate was set by good old BP (Sec. 5.4) in deep but otherwise standard NNs (Ciresan et al., 2010), using neither unsupervised pre-training (e.g., Sec. 5.7, 5.9, 5.14) nor convolution (e.g., Sec. 5.3, 5.5, 5.13). However, training pattern deformations (e.g., Sec. 5.13) were important to generate a big training set and avoid overfitting. This success was made possible mainly through a GPU implementation of BP that was up to 50 times faster than standard CPU versions. A good value of 0.95% was obtained without distortions except for small saccadic eye movement-like translations—compare Sec. 5.14.

Since BP was 3-5 decades old by then (Sec. 5.4), and pattern deformations 2 decades (Baird, 1990) (Sec. 5.13), these results seemed to suggest that advances in exploiting modern computing hardware were more important than advances in algorithms.

5.17 2011: Max-Pooling (MP) CNNs on GPU / Superhuman Vision Performance

In 2011, the first *GPU-implementation* (Ciresan et al., 2011a) of *Max-Pooling CNNs/Convnets* (GPU-MPCNNs) was described, building on earlier (MP)CNN work (Sec. 5.3, 5.5, 5.12), and on early GPU-based CNNs without MP (Chellapilla et al., 2006) (Sec. 5.14); compare GPU-DBNs (Raina et al., 2009) (Sec. 5.14) and early GPU-NNs (Oh and Jung, 2004). MPCNNs have alternating convolutional layers (Sec. 5.3) and max-pooling layers (MP, Sec. 5.12) topped by standard fully connected layers. All weights are trained by BP (Sec. 5.4, 5.5) (LeCun et al., 1989; Ranzato et al., 2007; Scherer et al., 2010). GPU-MPCNNs have become essential for many contest-winning FNNs (Sec. 5.19, Sec. 5.20).

Multi-Column (MC) GPU-MPCNNs (Ciresan et al., 2011b) are committees (Breiman, 1996; Schapire, 1990; Wolpert, 1992; Hashem and Schmeiser, 1992; Ueda, 2000; Dietterich, 2000a) of GPU-MPCNNs with simple democratic output averaging. Several MPCNNs see the same input; their output vectors are used to assign probabilities to the various possible classes. The class with the on average highest probability is chosen as the system's classification of the present input. Compare earlier, more sophisticated ensemble methods (Schapire, 1990), and the contest-winning ensemble Bayes-NN (Neal, 2006) of Sec. 5.13.

An MC-GPU-MPCNN was the first system to achieve superhuman visual pattern recognition (Ciresan et al., 2012b, 2011b) in a controlled competition, namely, the IJCNN 2011 traffic sign recognition contest in San Jose (CA) (Stallkamp et al., 2011). This is of interest for fully autonomous, self-driving cars in traffic, e.g., (Dickmanns et al., 1994). The MC-GPU-MPCNN obtained 0.56% error rate and was twice better than human test subjects, three times better than the closest artificial NN competitor (Sermanet and LeCun, 2011), and six times better than the best non-neural method.

A few months earlier, the qualifying round was won in a 1st stage online competition, albeit by a much smaller margin: 1.02% (Ciresan et al., 2011b) vs 1.03% for second place (Sermanet and LeCun, 2011). After the deadline, the organisers revealed that human performance on the test set was 1.19%. That is, the best methods already seemed human-competitive. However, during the qualifying it was possible to incrementally gain information about the test set by probing it through repeated submissions. This is illustrated by better and better results obtained by various teams over time (Stallkamp et al., 2011) (the organisers eventually imposed a limit of 10 resubmissions). In the final competition this was not possible.

This illustrates a general problem with benchmarks whose test sets are public, or at least can be probed to some extent: competing teams tend to overfit on the test set even when it cannot be directly used for training, only for evaluation.

In 1997 many thought it a big deal that human chess world champion Kasparov was beaten by an IBM computer. But back then computers could not at all compete with little kids in visual pattern recognition, which seems much harder than chess from a computational perspective. Of course, the traffic sign domain is highly restricted, and kids are still much better general pattern recognisers. Nevertheless, by 2011, deep NNs could already learn to rival them in important limited visual domains.

An MC-GPU-MPCNN also was the first method to achieve human-competitive performance (around 0.2%) on MNIST (Ciresan et al., 2012c).

Given all the prior work on (MP)CNNs (Sec. 5.3, 5.5, 5.12) and GPU-CNNs (Sec. 5.14), GPU-MPCNNs are not a breakthrough in the scientific sense. But they are a commercially relevant breakthrough in efficient coding that has made a difference in several contests since 2011. Today, GPU-MPCNNs are used by most if not all *feedforward* competition-winning deep NNs (Sec. 5.19, Sec. 5.20).

5.18 2011: Hessian-Free Optimization for RNNs

Also in 2011 it was shown (Martens and Sutskever, 2011) that Hessian-free optimization, e.g., (Møller, 1993; Pearlmutter, 1994; Schraudolph, 2002) (Sec. 5.6.2), can alleviate the *Fundamental Deep Learning Problem* (Sec. 5.8) in RNNs, outperforming standard LSTM RNNs (Sec. 5.11) on several tasks. Compare other RNN (Jaeger, 2004; Pascanu et al., 2013b; Koutník et al., 2014) that also at least sometimes yield better results than LSTM.

5.19 2012: First Contests Won on Object Detection / Segmentation / ImageNet

In 2012, an ensemble-based (Breiman, 1996; Schapire, 1990; Wolpert, 1992; Dietterich, 2000a) Multi-Column (MC, Sec. 5.17, 5.13) variant of a GPU-MPCNN (Sec. 5.17) also achieved best results (Krizhevsky et al., 2012) on the *ImageNet* classification benchmark, which is popular in the computer vision community. Here relatively large image sizes of 256x256 pixels were necessary, as opposed to only 48x48 pixels for the traffic sign competition (Sec. 5.17).

Also in 2012, the biggest NN so far (10^9 free parameters) was trained in unsupervised mode (Sec. 5.7, 5.14) on unlabeled data (Le et al., 2012), then applied to ImageNet. The codes across its top layer were used to train a simple supervised classifier, which achieved best results so far on 20,000 classes. Instead of relying on efficient GPU programming, this was done by brute force on 1,000 standard machines with 16,000 cores.

So by 2011/2012, excellent results had been achieved by Deep Learners in image *recognition and classification* (Sec. 5.17, 5.19). The computer vision community, however, is especially interested in *object detection* in large images, for applications such as image-based search engines, or for biomedical diagnosis where the goal may be to automatically detect tumors etc in images of human tissue. Object detection presents additional challenges. One natural approach is to train a deep NN classifier on patches of big images, then use it as a feature detector to be shifted across unknown visual scenes, using various rotations and zoom factors. Image parts that yield highly active output units are likely to contain objects similar to those the NN was trained on.

2012 finally saw the first DL system (an MC-GPU-MPCNN, Sec. 5.17) to win a contest on visual *object detection* in large images of several million pixels (ICPR 2012 Contest on Mitosis Detection in Breast Cancer Histological Images., 2012; Roux et al., 2013; Ciresan et al., 2013). Such biomedical applications may turn out to be among the most important applications of DL. The world spends over 10% of GDP on healthcare (> 6 trillion USD per year), much of it on medical diagnosis through expensive experts. Partial automation of this could not only save lots of money, but also make expert diagnostics accessible to many who currently cannot afford it. It is gratifying to observe that today deep NNs may actually help to improve healthcare and perhaps save human lives.

2012 also saw the first pure *image segmentation* contest won by DL, again through an MC-GPU-MPCNN (Segmentation of Neuronal Structures in EM Stacks Challenge, 2012; Ciresan et al., 2012a). (It should be mentioned, however, that LSTM RNNs already performed simultaneous segmentation and recognition when they became the first recurrent Deep Learners to win official international pattern recognition contests—Sec. 5.15.) EM stacks are relevant for the recently approved huge brain projects in Europe and the US. Given electron microscopy images of stacks of thin slices of animal brains, the goal is to build a detailed 3D model of the brain's neurons and dendrites. But human experts need many hours and days and weeks to annotate the images: Which parts depict neuronal membranes? Which parts are irrelevant background? This needs to be automated, e.g., (Turaga et al., 2010). Deep MC-GPU-MPCNNs learned to solve this task through experience with many training images, and won the contest on all three evaluation metrics by a large margin, with superhuman performance in terms of pixel error.

Both object detection (Ciresan et al., 2013) and image segmentation (Ciresan et al., 2012a) profit from fast MPCNN-based image scans that avoid redundant computations. Recent methods speed up naive implementations by three orders of magnitude (Masci et al., 2013b,a).

Also in 2012, on the IAM-OnDoDB benchmark, LSTM RNNs (Sec. 5.11) outperformed all other methods (HMMs, SVMs) on online mode detection (Otte et al., 2012; Indermuhle et al., 2012) and keyword spotting (Indermuhle et al., 2011). On the long time lag problem of language modelling, LSTM outperformed all statistical approaches on the IAM-DB benchmark (Frinken et al., 2012).

5.20 2013: More Contests and Benchmark Records

A stack (Fernandez et al., 2007; Graves and Schmidhuber, 2009) (Sec. 5.9) of bi-directional LSTM recurrent NNs (Graves and Schmidhuber, 2005) trained by CTC (Sec. 5.11, 5.15) broke a famous TIMIT speech (phoneme) recognition record, achieving 17.7% test set error rate (Graves et al., 2013), despite thousands of man years previously spent on *Hidden Markov Model* (HMMs)-based speech recognition research. Compare earlier DBN results (Sec. 5.14). CTC-LSTM also helped to score first at NIST's OpenHaRT2013

evaluation (Bluche et al., 2014). For *Optical Character Recognition* (OCR), LSTM RNNs outperformed commercial recognizers of historical data (Breuel et al., 2013).

A new record on the *ICDAR Chinese handwriting recognition benchmark* (over 3700 classes) was set on a desktop machine by an MC-GPU-MPCNN (Sec. 5.17) with almost human performance (Ciresan and Schmidhuber, 2013).

The *MICCAI 2013 Grand Challenge on Mitosis Detection* (Veta et al., 2013) also was won by an object-detecting MC-GPU-MPCNN (Ciresan et al., 2013). Its data set was even larger and more challenging than the one of ICPR 2012 (Sec. 5.19): a real-world dataset including many ambiguous cases and frequently encountered problems such as imperfect slide staining.

Deep GPU-MPCNNs (Sec. 5.17) also helped to achieve new best results on ImageNet classification (Zeiler and Fergus, 2013) and PASCAL object detection (Girshick et al., 2013), previously mentioned important benchmarks of the computer vision community. Compare additional work on object detection (Szegedy et al., 2013) and scene parsing (Farabet et al., 2013).

Additional contests are mentioned in the web pages of the Swiss AI Lab IDSIA, the University of Toronto, NY University, and the University of Montreal. (Unlike in most academic contests, winners of contests listed at the commercial web site *kaggle.com* have to hand their code over to companies.)

5.20.1 Currently Successful Supervised Techniques: LSTM RNNs / GPU-MPCNNs

Most competition-winning or benchmark record-setting Deep Learners actually use one of two *supervised* techniques: (a) recurrent LSTM (1997) trained by CTC (2006) (Sec. 5.11, 5.15, 5.19, 5.20), or (b) feedforward GPU-MPCNNs (2011, Sec. 5.17, 5.19, 5.20) building on earlier work since the 1960s (Sec. 5.4, 5.3, 5.5, 5.12). Exceptions include two 2011 contests specialised on *transfer learning* (Goodfellow et al., 2011; Mesnil et al., 2011; Goodfellow et al., 2012)—but compare SL-based transfer in deep NN (Ciresan et al., 2012d).

Remarkably, in the 1990s a trend went from partially unsupervised RNN stacks (Sec. 5.9) to purely supervised LSTM RNNs (Sec. 5.11), just like in the 2000s a trend went from partially unsupervised FNN stacks (Sec. 5.14) to purely supervised MPCNNs (Sec. 5.17–5.20).

Nevertheless, in many applications it can still be advantageous to combine the best of both worlds - *supervised* learning and *unsupervised* pre-training (Sec. 5.9, 5.14).

5.21 Recent Tricks for Improving SL Deep NNs (Compare Sec. 5.6.2, 5.6.3)

Rectified Linear Units (ReLU) clamp negative activations to zero ($f(x) = x$ if $x > 0$, $f(x) = 0$ otherwise). ReLU NNs are useful for RBMs (Nair and Hinton, 2010; Maas et al., 2013), outperformed sigmoidal activation functions in deep NNs (Glorot et al., 2011), and helped to obtain best results on several benchmark problems across multiple domains, e.g., (Krizhevsky et al., 2012; Dahl et al., 2013).

Maxout NNs (Goodfellow et al., 2013) combine competitive interactions and *dropout* (Hinton et al., 2012b) to achieve excellent results on certain benchmarks. Dropout removes units from NNs during training to improve generalisation. Some view it as an ensemble method that trains multiple data models simultaneously (Baldi and Sadowski, 2013). Under certain circumstances, it could also be viewed as a form of training set augmentation: effectively, more and more informative complex features are removed from the training data. Compare dropout for RNNs (Pham et al., 2013; Pachitariu and Sahani, 2013; Pascanu et al., 2013a). A deterministic approximation coined “fast dropout” (Wang and Manning, 2013) can lead to faster learning and evaluation and was adapted for RNNs (Bayer et al., 2013). Dropout is closely related to older, biologically plausible techniques of adding noise to neurons or synapses during training, e.g., (Murray and Edwards, 1993; Schuster, 1992; Nadal and Parga, 1994; Jim et al., 1995; An, 1996), which in turn are closely related to finding perturbation-resistant low-complexity NNs, e.g., through FMS (Sec. 5.6.3). MDL-based stochastic variational methods (Graves, 2011) are also related to FMS. They are useful for RNNs, where classic regularizers such as weight decay (Sec. 5.6.3) represent a bias towards limited memory capacity, e.g., (Pascanu et al., 2013b).

NNs with competing linear units tend to outperform those with non-competing nonlinear units, and avoid catastrophic forgetting through BP when training sets change over time (Srivastava et al., 2013).

In this context, choosing a learning algorithm may be more important than choosing activation functions (Goodfellow et al., 2014). Compare early RNNs with competing units for SL and RL (Schmidhuber, 1989b). To address overfitting, instead of depending on pre-wired regularizers and hyper-parameters (Hertz et al., 1991; Bishop, 2006), self-delimiting RNNs (SLIM NNs) with competing units (Schmidhuber, 2012) can in principle learn to select their own runtime and their own numbers of effective free parameters, thus learning their own computable regularisers (Sec. 4.3, 5.6.3), becoming fast and *slim* when necessary. One may penalize the task-specific total length of connections (Legenstein and Maass, 2002) and communication costs of SLIM NNs implemented on the 3-dimensional brain-like multi-processor hardware to expected in the future.

RmsProp (Tieleman and Hinton, 2012; Schaul et al., 2013) can improve first order gradient descent methods (Sec. 5.4, 5.6.2); compare *vario- η* (Neuneier and Zimmermann, 1996), *Adagrad* (Duchi et al., 2011) and *Adadelta* (Zeiler, 2012). Many additional, older tricks (Sec. 5.6.2, 5.6.3) should also be applicable to today's deep NNs; compare (Orr and Müller, 1998; Montavon et al., 2012).

5.22 Consequences for Neuroscience

It is ironic that artificial NNs (ANNs) can help to better understand biological NNs (BNNs)—see the ISBI 2012 results mentioned in Sec. 5.19 (Segmentation of Neuronal Structures in EM Stacks Challenge, 2012; Ciresan et al., 2012a). The feature detectors invented by deep visual ANNs should also be highly predictive of what neuroscientists will find in deep layers of BNNs. While the visual cortex of BNNs may use a quite different learning algorithm, its objective function to be minimised must be similar to the one of visual ANNs. Compare (Lee et al., 2007b; Yamins et al., 2013).

5.23 DL with Spiking Neurons?

Many recent DL results profit from GPU-based traditional deep NNs, e.g., (Sec. 5.14 - 5.17). Current GPUs, however, are little ovens, much hungrier for energy than biological brains, whose neurons efficiently communicate by brief spikes (Hodgkin and Huxley, 1952; FitzHugh, 1961; Nagumo et al., 1962), and often remain quiet. Many computational models of such *spiking neurons* have been proposed and analyzed, e.g., (Gerstner and van Hemmen, 1992; Zipser et al., 1993; Stemmler, 1996; Tsodyks et al., 1996; Maex and Orban, 1996; Maass, 1996, 1997; Kistler et al., 1997; Amit and Brunel, 1997; Kempter et al., 1999; Song et al., 2000; Stoop et al., 2000; Brunel, 2000; Bohte et al., 2002; Gerstner and Kistler, 2002; Izhikevich et al., 2003; Seung, 2003; Deco and Rolls, 2005; Brette et al., 2007; Kasabov, 2014). Future energy-efficient hardware for DL in NNs may implement aspects of such models; see, e.g., (Liu et al., 2001; Roggen et al., 2003; Glackin et al., 2005; Fieres et al., 2008; Khan et al., 2008; Serrano-Gotarredona et al., 2009; Jin et al., 2010). Current artificial networks of spiking neurons, however, cannot yet compete with the best traditional deep NNs in practical applications.

6 DL in FNNs and RNNs for Reinforcement Learning (RL)

So far we have focused on Deep Learning (DL) in supervised or unsupervised NNs. Such NNs learn to perceive / encode / predict / classify patterns or pattern sequences, but they do not learn to act in the more general sense of *Reinforcement Learning* (RL) in unknown environments, e.g., (Kaelbling et al., 1996; Sutton and Barto, 1998). Here we add a discussion of DL FNNs and RNNs for RL. It will be shorter than the discussion of FNNs and RNNs for SL and UL (Sec. 5), reflecting the current size of the various fields.

Without a teacher, solely from occasional real-valued pain and pleasure signals, RL agents must discover how to interact with a dynamic, initially unknown environment to maximize their expected cumulative reward signals (Sec. 2). There may be arbitrary, a priori unknown delays between actions and perceivable consequences. The problem is as hard as any problem of computer science, since any task with a computable description can be formulated in the RL framework, e.g., (Hutter, 2005). For example, an answer to the famous question of whether $P = NP$ (Levin, 1973b; Cook, 1971) would also set limits for what is achievable by general RL.

The following sections mostly focus on certain obvious intersections of DL and RL—they cannot serve as a general RL survey.

6.1 RL Through NN World Models Yields RNNs With Deep CAPs

In the special case of an RL NN controller C interacting with a *deterministic* environment, a separate FNN called M can learn to become C 's world model, predicting C 's inputs from previous actions and inputs, e.g., (Werbos, 1981, 1987; Munro, 1987; Jordan, 1988; Werbos, 1989b,a; Robinson and Fallside, 1989; Jordan and Rumelhart, 1990; Schmidhuber, 1990d; Narendra and Parthasarathy, 1990; Werbos, 1992; Gomi and Kawato, 1993; Cochocki and Unbehauen, 1993; Levin and Narendra, 1995; Ljung, 1998; Ge et al., 2010). Assume M has learned to produce accurate predictions. We can use M to substitute the environment. Then M and C form an RNN. Now BP for RNNs (Sec. 5.4.1) can be used to achieve desired input events such as high real-valued reward signals: While M 's weights remain fixed, gradient information for C 's weights is propagated back through M down into C and back through M etc. To a certain extent, the approach is also applicable in probabilistic or uncertain environments, as long as the inner products of M 's C -based gradient estimates and M 's “true” gradients tend to be positive.

In general, this approach implies deep CAPs for C , unlike in DP-based traditional RL (Sec. 6.2). The approach was used to learn to back up a model truck (Nguyen and Widrow, 1989). An RL active vision system used it to learn sequential shifts of a fovea to detect targets in visual scenes (Schmidhuber and Huber, 1991).

To allow for an M with memories of previous events in *partially observable worlds* (Sec. 6.3), the most general variant of this approach uses an RNN instead of an FNN as world model (Schmidhuber, 1990d, 1991c). This may cause deep CAPs not only for C but also for M . M can also be used to optimise expected reward by *planning* future action sequences (Schmidhuber, 1990d). In fact, the winners of the 2004 RoboCup World Championship in the fast league (Egorova et al., 2004) trained NNs to predict the effects of steering signals on fast robots with 4 motors for 4 different wheels. During play, such NN models were used to achieve desirable subgoals, by optimising action sequences through quickly planning ahead. The approach also was used to create *self-healing* robots able to compensate for faulty motors whose effects do not longer match the predictions of the NN models (Gloye et al., 2005; Schmidhuber, 2007).

Typically M is not given in advance. Then an essential question is: which experiments should C conduct to quickly improve M ? The *Formal Theory of Fun and Creativity* (Schmidhuber, 2006a, 2013b) formalizes driving forces and value functions behind such curious and exploratory behavior: A measure of the *learning progress* of M becomes the intrinsic reward of C (Schmidhuber, 1991a); compare (Singh et al., 2005; Oudeyer et al., 2013). This motivates C to create action sequences (experiments) such that M makes quick progress.

6.2 Deep FNNs for Traditional RL and Markov Decision Processes (MDPs)

The classical approach to RL (Samuel, 1959; Bertsekas and Tsitsiklis, 1996; Sutton and Barto, 1998) makes the simplifying assumption of *Markov Decision Processes* (MDPs): the current input of the RL agent con-

veys all information necessary to compute an optimal next output event or decision. This allows for greatly reducing CAP depth in RL NNs (Sec. 3, 6.1) by using the *Dynamic Programming* (DP) trick (Bellman, 1957). The latter is often explained in a probabilistic framework, e.g., (Sutton and Barto, 1998), but its basic idea can already be conveyed in a deterministic setting. For simplicity, using the notation of Sec. 2, let input events x_t encode the entire current state of the environment including a real-valued reward r_t (no need to introduce additional vector-valued notation, since real values can encode arbitrary vectors of real values). The original RL goal (find weights that maximize the sum of all rewards of an episode) is replaced by an equivalent set of alternative goals set by a real-valued value function V defined on input events. Consider any two subsequent input events x_t, x_k . Recursively define $V(x_t) = r_t + V(x_k)$, where $V(x_k) = r_k$ if x_k is the *last* input event. The goal is to find weights that maximize the V of all input events, by causing appropriate output events or actions.

Due to the Markov assumption, an FNN suffices to implement the policy that maps input to output events. Relevant CAPs are not deeper than this FNN. V itself is often modeled by a *separate FNN* (also yielding typically short CAPs) learning to approximate $V(x_t)$ only from *local* information $r_t, V(x_k)$.

Many variants of traditional RL exist, e.g., (Barto et al., 1983; Watkins, 1989; Watkins and Dayan, 1992; Moore and Atkeson, 1993; Schwartz, 1993; Baird, 1994; Rummery and Niranjan, 1994; Singh, 1994; Baird, 1995; Kaelbling et al., 1995; Peng and Williams, 1996; Mahadevan, 1996; Tsitsiklis and van Roy, 1996; Bradtke et al., 1996; Santamaría et al., 1997; Sutton and Barto, 1998; Wiering and Schmidhuber, 1998b; Baird and Moore, 1999; Meuleau et al., 1999; Morimoto and Doya, 2000; Bertsekas, 2001; Brafman and Tennenholtz, 2002; Abounadi et al., 2002; Lagoudakis and Parr, 2003; Sutton et al., 2008; Maei and Sutton, 2010). Most are formulated in a probabilistic framework, and evaluate pairs of input and output (action) events (instead of input events only). To facilitate certain mathematical derivations, some discount delayed rewards (but such distortions of the original RL problem are problematic).

Perhaps the most well-known RL NN is the world-class RL backgammon player Tesauro (1994), which achieved the level of human world champions by playing against itself. Its nonlinear, rather shallow FNN maps a large but finite number of discrete board states to values. More recently, a rather deep GPU-MPCNN (Sec. 5.17) was used in a traditional RL framework to learn to play several Atari 2600 computer games directly from 84x84 pixel video input (Mnih et al., 2013), using experience replay (Lin, 1993), extending previous work on *Neural Fitted Q-Learning* (NFQ) (Riedmiller, 2005). Compare earlier RL Atari players (Grüttner et al., 2010) and an earlier, raw video-based RL NN for computer games (Koutník et al., 2013) trained by *Indirect Policy Search* (Sec. 6.7).

6.3 Deep RL RNNs for Partially Observable MDPs (POMDPs)

The *Markov assumption* (Sec. 6.2) is often unrealistic. We cannot directly perceive what is behind our back, let alone the current state of the entire universe. However, memories of previous events can help to deal with *partially observable Markov decision problems* (POMDPs), e.g., (Schmidhuber, 1991c; Ring, 1991, 1993, 1994; Williams, 1992; Lin, 1993; Teller, 1994; Schmidhuber, 1995; Kaelbling et al., 1995; Littman et al., 1995; Boutilier and Poole, 1996; Littman, 1996; Jaakkola et al., 1995; McCallum, 1996; Kimura et al., 1997; Wiering and Schmidhuber, 1996, 1998a). A naive way of implementing memories without leaving the MDP framework (Sec. 6.2) would be to simply consider a possibly huge state space, namely, the set of all possible observation histories and their prefixes. A more realistic way is to use function approximators such as RNNs that produce compact state features as a function of the entire history seen so far. Generally speaking, POMDP RL often uses DL RNNs to learn which events to memorize and which to ignore. Three basic alternatives are:

1. Use an RNN as a value function mapping arbitrary event histories to values, e.g., (Schmidhuber, 1990b, 1991c; Lin, 1993; Bakker, 2002). For example, deep LSTM RNNs were used in this way for RL robots (Bakker et al., 2003).
2. Use an RNN controller in conjunction with a second RNN as predictive world model, to obtain a combined RNN with deep CAPs—see Sec. 6.1.
3. Use an RNN for RL by *Direct Search* (Sec. 6.6) or *Indirect Search* (Sec. 6.7) in weight space.

In general, however, POMDPs may imply greatly increased CAP depth.

6.4 RL Facilitated by Deep UL

RL machines may profit from UL for input preprocessing, e.g., (Jodogne and Piater, 2007). In particular, an UL NN can learn to compactly encode environmental inputs such as images or videos, e.g., Sec. 5.7, 5.9, 5.14. The compact codes (instead of the high-dimensional raw data) can be fed into an RL machine, whose job thus may become much easier (Legenstein et al., 2010; Cuccu et al., 2011), just like SL may profit from UL, e.g., Sec. 5.7, 5.9, 5.14. For example, NFQ (Riedmiller, 2005) was applied to real-world control tasks (Lange and Riedmiller, 2010; Riedmiller et al., 2012) where purely visual inputs were compactly encoded by deep autoencoders (Sec. 5.7, 5.14). RL combined with UL based on *Slow Feature Analysis* (Wiskott and Sejnowski, 2002; Kompella et al., 2012) enabled a real humanoid robot to learn skills from raw high-dimensional video streams (Luciw et al., 2013). To deal with POMDPs (Sec. 6.3), a RAAM (Pollack, 1988) (Sec. 5.7) was employed as a deep unsupervised sequence encoder for RL (Gisslen et al., 2011).

6.5 Deep Hierarchical RL (HRL) and Subgoal Learning

Multiple learnable levels of abstraction (Fu, 1977; Lenat and Brown, 1984; Ring, 1994; Bengio et al., 2013; Deng and Yu, 2014) seem as important for RL as for SL. Work on NN-based hierarchical RL (HRL) has been published since the early 1990s. In particular, gradient-based subgoal discovery with FNNs or RNNs decomposes RL tasks into subtasks for RL submodules (Schmidhuber, 1991b; Schmidhuber and Wahnsiedler, 1992). Numerous alternative HRL techniques have been proposed, e.g., (Ring, 1991, 1994; Tenenbergs et al., 1993; Moore and Atkeson, 1995; Precup et al., 1998; Dietterich, 2000b; Menache et al., 2002; Doya et al., 2002; Ghavamzadeh and Mahadevan, 2003; Barto and Mahadevan, 2003; Samejima et al., 2003; Bakker and Schmidhuber, 2004; Whiteson et al., 2005; Simsek and Barto, 2008). While HRL frameworks such as Feudal RL (Dayan and Hinton, 1993) and options (Sutton et al., 1999b; Barto et al., 2004; Singh et al., 2005) do not directly address the problem of automatic subgoal discovery, HQ-learning (Wiering and Schmidhuber, 1998a) automatically decomposes POMDPs (Sec. 6.3) into sequences of simpler subtasks that can be solved by memoryless policies learnable by reactive sub-agents. Recent HRL organizes potentially deep NN RL sub-modules into self-organizing, 2-dimensional motor control maps (Ring et al., 2011) inspired by neurophysiological findings (Graziano, 2009).

6.6 Deep RL by Direct NN Search / Policy Gradients / Evolution

Not quite as universal as the methods of Sec. 6.8, yet both practical and more general than most traditional RL algorithms (Sec. 6.2), are methods for *Direct Policy Search* (DS). Without a need for value functions or Markovian assumptions (Sec. 6.2, 6.3), the weights of an FNN or RNN are directly evaluated on the given RL problem. The results of successive trials inform further search for better weights. Unlike with RL supported by BP (Sec. 5.4, 6.3, 6.1), CAP depth (Sec. 3, 5.8) is not a crucial issue. DS may solve the credit assignment problem without backtracking through deep causal chains of modifiable parameters—it neither cares for their existence, nor tries to exploit them.

An important class of DS methods for NNs are policy gradient methods (Williams, 1986, 1988, 1992; Baxter and Bartlett, 1999; Sutton et al., 1999a; Aberdeen, 2003; Ghavamzadeh and Mahadevan, 2003; Kohl and Stone, 2004; Wierstra et al., 2007, 2008; Rückstieß et al., 2008; Peters and Schaal, 2008b,a; Sehnke et al., 2010; Grüttner et al., 2010; Wierstra et al., 2010; Peters, 2010; Bartlett and Baxter, 2011; Grondman et al., 2012). Gradients of the total reward with respect to policies (NN weights) are estimated (and then exploited) through repeated NN evaluations.

RL NNs can also be evolved through *evolutionary algorithms* (EAs) (Rechenberg, 1971; Schwefel, 1974; Holland, 1975; Fogel et al., 1966; Smith, 1980; Cramer, 1985; Goldberg, 1989) in a series of trials. Here several policies are represented by a population of NNs improved by repeatedly recombining the population's fittest individuals. Compare probability distribution-based EAs (Baluja, 1994; Saravanan and Fogel, 1995; Sałustowicz and Schmidhuber, 1997; Larraanaga and Lozano, 2001) and *Covariance Matrix Estimation Evolution Strategies* (CMA-ES) (Hansen and Ostermeier, 2001; Hansen et al., 2003; Igel, 2003). Many RNN evolvers have been proposed (Miller et al., 1989; Yao, 1993; Nolfi et al., 1994; Sims, 1994; Yamauchi and Beer, 1994; Miglino et al., 1995; Moriarty, 1997; Pasemann et al., 1999; Juang,

2004). One particularly effective family of methods *coevolves* neurons, combining them into networks, and selecting those neurons for reproduction that participated in the best-performing networks (Moriarty and Miikkulainen, 1996; Gomez, 2003; Gomez and Miikkulainen, 2003). This can help to solve deep POMDPs (Gomez and Schmidhuber, 2005). *Co-Synaptic Neuro-Evolution* (CoSyNE) does something similar on the level of synapses or weights (Gomez et al., 2008); benefits of this were shown on difficult non-linear POMDP benchmarks.

Natural Evolution Strategies (NES) (Wierstra et al., 2008; Glasmachers et al., 2010; Sun et al., 2009, 2013) link policy gradient methods and evolutionary approaches through the concept of natural gradients (Amari, 1998). RNN evolution may also help to improve SL for deep RNNs through *Evolino* (Schmidhuber et al., 2007) (Sec. 5.8).

6.7 Deep RL by Compressed NN Search

Some DS methods (Sec. 6.6) can evolve NNs with hundreds of weights, but not millions. How to search for large and deep NNs? Most SL and RL methods mentioned so far somehow search the space of weights w_i . Some profit from a reduction of the search space through shared w_i that get reused over and over again, e.g., in CNNs (Sec. 5.3, 5.5, 5.19), or in RNNs for SL (Sec. 5.4, 5.11) and RL (Sec. 6.6).

It may be possible, however, to exploit *additional* regularities/compressibilities in the space of solutions, through *indirect search in weight space*. Instead of evolving large NNs directly (Sec. 6.6), one can sometimes greatly reduce the search space by evolving *compact encodings* of NNs, e.g., through *Lindenmeyer Systems* (Lindenmayer, 1968; Jacob et al., 1994), *graph rewriting* (Kitano, 1990), *Cellular Encoding* (Gruau et al., 1996), *NeuroEvolution of Augmenting Topologies* (NEAT) (Stanley and Miikkulainen, 2002), and HyperNEAT (D’Ambrosio and Stanley, 2007; Stanley et al., 2009; Clune et al., 2011). This helps to avoid overfitting (compare Sec. 5.6.3, 5.21) and is closely related to the topics of regularisation and MDL (Sec. 4.3).

A general approach (Schmidhuber, 1995) for both SL and RL seeks to compactly encode weights of large NNs (Schmidhuber, 1997) through programs written in a *universal programming language* (Gödel, 1931; Church, 1936; Turing, 1936; Post, 1936). Often it is much more efficient to systematically search the space of such programs with a bias towards short and fast programs (Levin, 1973b; Schmidhuber, 1995, 1997, 2004), instead of directly searching the huge space of possible NN weight matrices. A previous universal language for encoding NNs was assembler-like (Schmidhuber, 1995). More recent work uses more practical languages based on coefficients of popular transforms (Fourier, wavelet, etc). In particular, RNN weight matrices may be compressed like images, by encoding them through the coefficients of a *discrete cosine transform* (DCT) (Koutník et al., 2010, 2013). Compact DCT-based descriptions can be evolved through NES or CoSyNE (Sec. 6.6). An RNN with over a million weights learned (without a teacher) to drive a simulated car in the TORCS driving game (Loiacono et al., 2009, 2011), based on a high-dimensional video-like visual input stream (Koutník et al., 2013). The RNN learned both control and visual processing from scratch, without being aided by UL. (Of course, UL might help to generate more compact image codes to be fed into a smaller RNN, to reduce the overall computational effort.)

6.8 Universal RL

General purpose learning algorithms may improve themselves in open-ended fashion and environment-specific ways in a lifelong learning context (Schmidhuber, 1987; Schmidhuber et al., 1997b,a; Schaul and Schmidhuber, 2010). The most general type of RL is constrained only by the fundamental limitations of computability identified by the founders of theoretical computer science (Gödel, 1931; Church, 1936; Turing, 1936; Post, 1936). Remarkably, there exist blueprints of *universal problem solvers* or *universal RL machines* for unlimited problem depth that are time-optimal in various theoretical senses (Hutter, 2005, 2002; Schmidhuber, 2002, 2006b). The *Gödel Machine* can be implemented on general computers such as RNNs and may improve any part of its software (including the learning algorithm itself) in a way that is provably time-optimal in a certain sense (Schmidhuber, 2006b). It can be initialized by an *asymptotically optimal* meta-method (Hutter, 2002) (also applicable to RNNs) which will solve any well-defined problem as quickly as the unknown fastest way of solving it, save for an additive constant overhead that becomes negligible as problem size grows. Note that most problems are large; only few are small. AI and DL

researchers are still in business because many are interested in problems so small that it is worth trying to reduce the overhead through less general methods (including heuristics). Here I won't further discuss universal RL methods, which go beyond what is usually called DL.

7 Conclusion

Deep Learning (DL) in *Neural Networks* (NNs) is relevant for *Supervised Learning* (SL) (Sec. 5), *Unsupervised Learning* (UL) (Sec. 5), and *Reinforcement Learning* (RL) (Sec. 6). By alleviating problems with deep *Credit Assignment Paths* (CAPs, Sec. 3, 5.8), UL (Sec. 5.6.4) cannot only facilitate SL of sequences (Sec. 5.9) and stationary patterns (Sec. 5.7, 5.14), but also RL (Sec. 6.4, 4.2). *Dynamic Programming* (DP, Sec. 4.1) is important for both deep SL (Sec. 5.4) and traditional RL with deep NNs (Sec. 6.2). A search for solution-computing, perturbation-resistant (Sec. 5.6.3, 5.14, 5.21), low-complexity NNs describable by few bits of information (Sec. 4.3) can reduce overfitting and improve deep SL & UL (Sec. 5.6.3, 5.6.4) as well as RL (Sec. 6.7), also in the case of partially observable environments (Sec. 6.3). Deep SL, UL, RL often create hierarchies of more and more abstract, less and less redundant representations of stationary data (Sec. 5.7, 5.14), sequential data (Sec. 5.9), or RL policies (Sec. 6.5). The future may belong to general purpose learning algorithms that improve themselves in provably optimal ways (Sec. 6.8), but these are not yet practical or commercially relevant. While UL can facilitate SL, pure SL for feedforward NNs (FNNs) (Sec. 5.4, 5.5, 5.16) and recurrent NNs (RNNs) (Sec. 5.4, 5.11) did not only win early contests (Sec. 5.10, 5.13), but also most of the recent ones (Sec. 5.15-5.20). DL FNNs profited from GPU implementations (Sec. 5.14 - 5.17). In particular, GPU-based (Sec. 5.17) Max-Pooling (Sec. 5.12) Convolutional NNs (Sec. 5.3, 5.5) won competitions not only in pattern recognition (Sec. 5.17 - 5.20) but also image segmentation (Sec. 5.19) and object detection (Sec. 5.19 - 5.20).

Acknowledgments

Thanks to numerous NN experts for valuable comments.

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